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Circular and rectilinear Sagnac effects are dynamically equivalent and contradictory to special relativity theory

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Abstract: The Sagnac effect, named after its discoverer, is the phase shift occurring between two beams of light, traveling in opposite directions along a closed path around a moving object. A special case is the circular Sagnac effect, known for its crucial role in the global positioning system (GPS) and fiber-optic gyroscopes. It is often claimed that the circular Sagnac effect does not contradict special relativity theory (SRT) because it is considered an accelerated motion, while SRT applies only to uniform, nonaccelerated motion. It is further claimed that the Sagnac effect, manifest in circular motion, should be treated in the framework of general relativity theory (GRT). We counter these arguments by underscoring the fact that the dynamics of rectilinear and circular types of motion are completely equivalent, and that this equivalence holds true for both nonaccelerated and accelerated motion. With respect to the Sagnac effect, this equivalence means that a uniform circular motion (with constant ω) is completely equivalent to a uniform rectilinear motion (with constant v). We support this conclusion by convincing experimental findings, indicating that an *identical* Sagnac effect to the one found in circular motion, exists in rectilinear uniform motion. We conclude that the circular Sagnac effect is fully explainable in the framework of inertial systems, and that the circular Sagnac effect contradicts SRT and calls for its refutation. © 2018 Physics Essays Publication. [<http://dx.doi.org/10.4006/0836-1398-31.2.215>]

Résumé: L'effet Sagnac, nommé d'après son découvreur, est le déphasage qui se produit entre deux faisceaux de lumière voyageant dans des sens opposés le long d'un chemin fermé autour d'un objet en mouvement. Un cas particulier est l'effet circulaire de Sagnac, connu pour son rôle crucial dans le système Global Positioning System (GPS) et les gyroscopes à fibre optique. On dit souvent que l'effet circulaire de Sagnac ne viole pas la théorie de la relativité restreinte, parce qu'il s'agirait d'un mouvement accéléré, alors que cette théorie ne s'applique qu'aux mouvements uniformes non accélérés. On dit aussi que l'effet Sagnac, qui se manifeste dans le mouvement circulaire, doit être traité dans le cadre de la théorie de la relativité générale. Nous allons à l'encontre de ces affirmations en soulignant le fait que les dynamiques des mouvements rectilignes et circulaires sont absolument équivalentes, et que cette équivalence vaut pour les mouvements aussi bien non accélérés qu'accélérés. En ce qui concerne l'effet Sagnac, cette équivalence signifie qu'un mouvement circulaire uniforme (à constante ω) est totalement équivalent à un mouvement rectiligne uniforme (à constante v). Nous soutenons cette conclusion par des résultats expérimentaux convaincants qui indiquent qu'un effet de Sagnac *identique* à celui trouvé dans le mouvement circulaire existe en mouvement rectiligne uniforme. Nous concluons que l'effet circulaire de Sagnac est pleinement explicable dans le cadre des systèmes inertiels, qu'il contredit la théorie de la relativité restreinte et qu'il appelle à la réfutation de cette théorie.

Key words: Sagnac Effect; Special Relativity Theory; Lorentz Invariance; Systems Equivalence; GPS.

I. INTRODUCTION

The Sagnac effect is a phase shift observed between two beams of light traveling in opposite directions along the same closed path around a moving object. Called after its discoverer in 1913,¹ the Sagnac effect has been replicated in many experiments.²⁻⁵

The circular Sagnac effect is a special case of the general Sagnac effect, which has crucial applications in fiber-optic gyroscopes (FOGs)⁶⁻¹⁰ and in navigation systems such as the global positioning system (GPS).^{2,11} The amount of the circular Sagnac effect is calculated using a Galilean summation of the velocity of light and the velocity of the rotating frame ($c \pm \omega r$). The difference in time intervals of two light beams sent clockwise and counterclockwise around a closed path on a rotating circular disk is $\Delta t = \frac{2v'l}{c^2}$, where $v = \omega R$ is the

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55 speed of the circular motion, and $l = 2\pi R$ is the circumfer- 112
 56 ence of the circle. In fact, the Galilean summation of c and 113
 57 $\pm wr$ contradict special relativity theory's (SRT's) second 114
 58 axiom and the Lorentz transformations. Nonetheless, it is 115
 59 consensual that the Sagnac effect does not falsify SRT,¹² 116
 60 because it is manifested in circular motion, which is consid- 117
 61 ered an accelerated motion,¹³⁻¹⁵ while SRT applies only to 118
 62 inertial (nonaccelerated) systems. Based on this consensus, 119
 63 in the GPS, concurrent corrections for the Sagnac effect and 120
 64 SRT's time dilation are made. Moreover, some theoreticians 121
 65 claimed that the Sagnac effect manifest in circular motion, 122
 66 should be treated in the framework of general relativity the-
 67 ory (GRT) and not SRT.^{16,17}

68 The view that the Sagnac effect is a property of rota- 123
 69 tional systems is strongly disproved by Wang and his 124
 70 colleagues¹⁸⁻²⁰ who conducted experiments demonstrating 125
 71 that an *identical* Sagnac effect, to the one found in circular 126
 72 motion, exists in rectilinear uniform motion.²¹ Using an opti- 127
 73 cal fiber conveyor, the authors measured the travel-time dif-
 74 ference between two counter propagating light beams in a
 75 uniformly moving fiber. Their finding revealed that the
 76 travel-time difference in a fiber segment of length Δl moving
 77 at a speed v was equal to $\Delta t = 2v\Delta l/c^2$, whether the segment
 78 was moving uniformly in rectilinear or circular motion. The
 79 existence of a Sagnac effect in rectilinear uniform motion is
 80 at odds with the prediction of SRT, and with the Lorentz
 81 invariance principle and, thus, should qualify as a strong ref-
 82 utation of both theories. However, despite the fact that Wang
 83 and his colleagues published their findings in well-respected
 84 mainstream journals, their falsification of SRT's second
 85 axiom, and the Lorentz transformations, has been completely
 86 ignored. To the best of my knowledge, no effort was done by
 87 SRT experimentalists to replicate Wang *et al.*'s falsifying
 88 test of SRT.

89 In this short note, we provide strong theoretical support 130
 90 to the aforementioned findings regarding the identity 131
 91 between the rectilinear and circular Sagnac effects, by under- 132
 92 scoring the fact that, in disagreement with the acceptable 133
 93 Newton's definition of inertial motion, the dynamics of 134
 94 rectilinear and circular types of motion are completely equiv- 135
 95 alent, and that this equivalence holds true for both nonaccel- 136
 96 erated and accelerated motion. We elucidate this fact in 137
 97 Section II and in Section III we draw conclusions regarding 138
 98 the contradiction between the rectilinear and circular Sagnac 139
 99 effects, and the predictions of SRT.

100 **II. ON THE EQUIVALENCE BETWEEN CIRCULAR AND**
 101 **RECTILINEAR KINEMATICS**

102 The common view in physics is that the above- 140
 103 mentioned two types of motion are, in general, qualitatively 141
 104 different. Linear motion with constant velocity is considered 142
 105 inertial, while circular motion, even with constant radial 143
 106 velocity, is considered an accelerated (noninertial) motion. 144
 107 The above view is not restricted to the Sagnac effect, or to 145
 108 relativistic motion, but it is believed to be a general distinc- 146
 109 tion in classical mechanics as well, and is repeated in all 147
 110 books on physics. This common view maintains that the cen- 148
 111 tripetal force acting on a rigid rotating mass causes continual

change in its velocity vector, reflected in change in its direc- 112
 tion (keeping it in a tangential direction to the circular path). 113

Here, we challenge this convention by claiming that 114
 there is a one-to-one correspondence between the linear and 115
 circular types of motion. In the language of systems analysis, 116
 the two types of motion are completely *equivalent* sys- 117
 tems.^{22,23} The proof for our claim is trivial. To verify that, 118
 consider a dynamical system of any type (physical, biological, 119
 social, etc.), which could be completely defined by a set 120
 of dynamical parameters p_i ($i = 1, 2, \dots, 6$), and a set of 121
 equations R defined as 122

$$R = \left\{ \begin{aligned} p_2 &= \dot{p}_1, p_3 = \ddot{p}_1, p_5 = p_3 p_4, \\ p_6 &= \int p_5 dp_1, p_7 = \frac{1}{2} p_4 p_2^2 \end{aligned} \right\} \quad (1)$$

If we think of p_1, p_2, p_3 , as representing rectilinear posi- 123
 tion x , velocity v , and acceleration a , respectively, and of p_4 , 124
 p_5, p_6, p_7 , as mass m , rectilinear force F , work W , and kinetic 125
 energy E , respectively, then the dynamical system defined by 126
 R gives a full description of a classical *rectilinear motion* 127
 (see Table I). Alternatively, if we think of p_1, p_2, p_3 , as rep- 128
 resenting angular position θ , velocity ω , and acceleration α , 129
 respectively, and of p_4, p_5, p_6, p_7 , as radial inertia I , torque τ , 130
 work W , and kinetic energy E , respectively, then the dynamical 131
 system defined by R gives a full description of a classical 132
circular motion (Q.E.D.). 133

It is worth noting that the equivalence between rectilin- 134
 ear and circular dynamical systems is not restricted to the 135
 special case of rotation with constant angular velocity or 136
 even with constant acceleration. 137

We note here that the equivalence demonstrated above 138
 between the dynamics of uniform rectilinear and uniform cir- 139
 cular types of motion is inconsistent with Newton's first law, 140
 which states that, *unless acted upon by a net unbalanced* 141
force, an object will remain at rest, or move uniformly 142
*forward in a straight line.*²⁴ According to this definition of 143
 inertial motion, which was adopted by Einstein, a circular 144
 motion with uniform radial velocity is considered an acceler- 145
 ated motion. However, the above demonstrated equivalence 146
 is at odds with Newton and Einstein's views of inertial sys- 147
 tems. In fact, based on Newton's mechanics, the first law for 148

TABLE I. Dynamical equations of rectilinear and circular systems.

Variable	Rectilinear	Circular	General
Position	x	θ	p_1
Velocity	$v = \frac{dx}{dt}$	$\omega = \frac{d\theta}{dt}$	$p_2 = \frac{dp_1}{dt}$
Acceleration	$a = \frac{dv}{dt}$	$\alpha = \frac{d\omega}{dt}$	$p_3 = \frac{dp_2}{dt}$
Mass/Inertia	M	I	p_4
Newton's second law	$F = ma$	$\tau = I\alpha$	$p_5 = p_4 p_3$
Work	$W = \int F dx$	$W = \int \tau d\theta$	$p_6 = \int p_5 dp_1$
Kinetic energy	$E = \frac{1}{2} mv^2$	$E = \frac{1}{2} I \omega^2$	$p_7 = \frac{1}{2} p_4 p_2^2$

149 circular motion could be derived simply by replacing, in the
 150 original statement of the law, the words “straight line” by the
 151 word “circle,” thus yielding the following law:

152 “A body in circular motion will continue its
 153 rotation in the same direction at a constant
 154 angular velocity unless disturbed.”

155 Quite interestingly, our view of what defines an inertial
 156 system is in complete agreement with Galileo’s interpreta-
 157 tion of inertia. In Galileo’s words: “All external impediments
 158 removed, a heavy body on a spherical surface concentric
 159 with the earth will maintain itself in that state in which it has
 160 been; if placed in movement toward the west (for example),
 161 it will maintain itself in that movement.”²⁵ This notion,
 162 which is termed “circular inertia” or “horizontal circular
 163 inertia” by historians of science, is a precursor to Newton’s
 164 notion of *rectilinear inertia*.^{26,27}

165 A deeper inquiry of the different opinions of the notion
 166 of “inertia” throughout the history of physics is beyond the
 167 scope and aims of the present paper. Nonetheless, we dare to
 168 put forward the following definition of an inertial motion,
 169 which agrees well with Galileo’s conception. According to
 170 the proposed definition, *a rigid body is said to be in a state*
 171 *of inertial motion if and only if the scalar product between*
 172 *the sum of all the forces acting on the body, and its velocity*
 173 *vector is always equal to zero, or*

$$\left(\sum \vec{F}_i(t) \right) \cdot \vec{v}(t) = 0 \text{ for all } t. \quad (2)$$

174 Note that the condition in Eq. (2) is satisfied (under ideal
 175 conditions) only by two types of motion: The rectilinear and
 176 the circular types of motion.

177 **III. CONCLUSIONS AND GENERAL REMARKS**

178 Although it is not the subject of the present paper, our dem-
 179 onstration of the complete equivalence between the circular
 180 and the rectilinear dynamics, based on Newtonian dynamics,
 181 calls for a reformulation of Newton’s first law, which is *in line*
 182 *with Galileo’s view of inertial motion. Such reformulation is*
 183 *far from being semantic.* By accepting the fact that the circular
 184 and rectilinear dynamics are completely equivalent, it becomes
 185 inevitable but to conclude that the Sagnac effect in uniform cir-
 186 cular motion is completely equivalent to the Sagnac effect in
 187 uniform rectilinear motion, and that both effects contradict
 188 SRT.

189 Moreover, the claim that the circular Sagnac effect
 190 should be treated in the framework of GRT simply does not
 191 make sense. *In most Sagnac experiments, the experimental*
 192 *apparatus is of small physical dimensions,* allowing us to
 193 assume that the gravitational field in the apparatus is uni-
 194 form, *thus excluding any GRT effects.*

195 Another erroneous justification for the coexistence
 196 between SRT and the Sagnac effect is that the observed
 197 effect could be derived from SRT,^{28,29} e.g., by using Lorentz
 198 transformations expressed in coordinates of a rotating frame.
 199 This claim is based on fact that the difference between the
 200 detected effect, and the one predicted by SRT, amounts to
 201 $\frac{1}{2}(\frac{v}{c})^2$, which is claimed to be negligible for all practical cases

and applications. We argue that this line of reasoning is erro-
 202 neous in more than one aspect: (1) *The directionality of the*
 203 *Sagnac effect is dependent on the direction of light travel*
 204 *with respect to the rotating object, whereas the time dilation*
 205 *effect is independent of the direction of motion;* (2) *Special*
 206 *relativity is founded on the axiom postulating that the motion*
 207 *of the source of light, relative to the detector, has no effect*
 208 *on the measured velocity of light, whereas in the Sagnac*
 209 *effect, the Galilean kinematic composition of velocities*
 210 *($c + v, c - v$) is the reason behind its appearance;* (3) *At rela-*
 211 *tivistic velocities, for which SRT predictions become practi-*
 212 *cally relevant, the second order of v/c can amount to values*
 213 *approaching one; and* (4) *The aforementioned difference,*
 214 *even if infinitesimally small, as in the case of GPS, could not*
 215 *be overlooked because it is a systematic deviation between*
 216 *the model’s prediction and reality, and not some kind of sta-*
 217 *tistical or system’s error.*

219 Finally, we note that the abundance of experimental
 220 findings in support of SRT, mainly its prediction of time
 221 dilation,^{30–33} is no more than what Carl Popper calls
 222 “confirmation tests” of the theory. *What is needed is to sub-*
 223 *ject SRT to stringent tests, i.e., to what Carl Popper has*
 224 *termed a “risky” or “severe” falsification test.*^{34,35} *Evidently,*
 225 *the Sagnac effect, arising in rectilinear and in circular*
 226 *motion, qualifies as a severe test of SRT. But such experi-*
 227 *ments have already been performed in linear and circular*
 228 *motion by Wang and his colleagues,^{18–20} and we have shown*
 229 *here that the two types of motion are completely equivalent.*

230 *We have no other way but to conclude that the physics*
 231 *community is acting irrationally and unscientifically.* The logic
 232 behind the second axiom of SRT is shaky, and Herbert Ding-
 233 le’s argument^{36–38} that it leads to contradiction has never
 234 been answered without violating the principle of relativity
 235 itself. On the experimental side, the Sagnac effect detected in
 236 linear motion is a clear falsification of the theory, and we have
 237 closed the loophole by showing here that what applies to recti-
 238 linear motion applies to circular motion.

239 In science, it takes one well-designed and replicated
 240 experiment to falsify a theory. As put most succinctly by
 241 Einstein himself: “If an experiment agrees with a theory it
 242 means ‘perhaps’ for the latter... but If it does not agree, it
 243 means ‘no’.”³⁹ (p. 203). Meanwhile, an experiment falsify-
 244 ing SRT is flying above our heads in the GPS and similar
 245 systems, but there are *no good and brave experimentalists*
 246 *to observe them and register their results.*

247 *We are not aware of a similar case in the history of*
 248 *modern science, where a theory, which defies reason, and*
 249 *contradicts with the findings of crucial tests, holds firm.* We
 250 believe that it is due time for a serious reconsideration of
 251 SRT and the Lorentz transformations.

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